Lebanese American University School of Arts and Sciences Department of Computer Science and Mathematics

CSC 320 - Computer Organization

Problem Set 1: Number Systems

Problem 1. Perform the following number system conversions:

(a) $1101011_2 = ?_{16}$ (b) $10100.1101_2 = ?_{16}$ (c) $101111.0111_2 = ?_8$ <u>Solution:</u> (a) $1101011 = 6B_{16}$ (b) $10100.1101 = 14.D_{16}$ (c) $101111.0111 = 57.34_8$

Problem 2. Convert the following octal numbers into binary and hexadecimal:

(a) $1234_8 = ?_2 = ?_{16}$ (b) $365517_8 = ?_2 = ?_{16}$ (c) $7436.11_8 = ?_2 = ?_{16}$

Solution: (a) $1234_8 = 1010011100_2 = 29C_{16}$ (b) $365517_8 = 11110101101001111_2 = 1EB4F_{16}$ (c) $7436.11_8 = 111100011110.001001_2 = F1E.24_{16}$

Problem 3. Convert the following hexadecimal numbers into binary and octal:

(a) $1023_{16} = ?_2 = ?_8$ (b) $ABCD_{16} = ?_2 = ?_8$ (c) $9E36.7A_{16} = ?_2 = ?_8$ <u>Solution:</u> (a) $1023_{16} = 1000000100011_2 = 10043_8$ (b) $ABCD_{16} = 1010101111001101_2 = 125715_8$ (c) $9E36.7A_{16} = 1001111000110110.0111101_2 = 117066.364_8$ Problem 4. Convert the following numbers into decimal:

(a) $12010_3 = ?_{10}$ (b) $7156_8 = ?_{10}$ (c) $15C.38_{16} = ?_{10}$ (d) $12010_3 = 138_{10}$ (b) $7156_8 = 3694_{10}$ (c) $15C.38_{16} = 348.21875_{10}$

Problem 5. Perform the following number-system conversions:

(a) $125_{10} = ?_2$ (b) $727_{10} = ?_5$ (c) $1435_{10} = ?_8$ <u>Solution:</u> (a) $125_{10} = 1111101_2$ (b) $727_{10} = 10402_5$ (c) $1435_{10} = 2633_8$

Problem 6. Each of the following arithmetic operations is correct in at least one number system. Determine possible radices of the numbers in each operation.

(a)
$$1234 + 5432 = 6666$$

(b) $41 / 3 = 13$
(c) $33 / 3 = 11$
(d) $23 + 44 + 14 + 32 = 223$
(e) $302 / 20 = 12.1$
(f) $\sqrt{41} = 5$
Solution:
(a) any b > 6
(b) b = 8
(c) any b > 3
(d) b = 5
(e) b = 4
(f) b = 6